# The Crystal Structure of KAu(CN)<sub>2</sub>\*

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### (Received 15 January 1959)

KAu(CN)<sub>2</sub> is rhombohedral, space group  $R\overline{3}$ , with a = 9.74 Å and  $\alpha = 43.9^{\circ}$ . The structure is similar to that of KAg(CN)<sub>2</sub> and consists of layers of linear Au(CN)<sub>2</sub><sup>-</sup> ions alternating with layers of K<sup>+</sup> ions. However, the stacking of the layers differs in the two compounds, so that KAg(CN)<sub>2</sub> is hexagonal and KAu(CN)<sub>2</sub> is rhombohedral. A refinement of the structure was made by least-squares analysis of counter data. The Au-C bond is  $2.12 \pm 0.14$  Å, the C-N bond is  $1.17 \pm 0.20$  Å and the average K-N distance is 2.78 Å. Twinned crystals of KAu(CN)<sub>2</sub> often occur and the nature of this twinning is discussed in detail.

## Introduction

As part of a study of complex metal cyanides, which is being conducted in this laboratory (see Cromer, 1957, for further references), the crystal structure of KAu(CN)<sub>2</sub>, has been determined. This compound has essentially the same structure as that of KAg(CN)<sub>2</sub> (Hoard, 1933) but, because of a different stacking sequence, the KAu(CN)<sub>2</sub> lattice is rhombohedral rather than hexagonal.

The space group of KAu(CN)<sub>2</sub> was reported by Staritzky & Ellinger (1956) to be R3 with a=9.74 Å and  $\alpha=43.9^{\circ}$ . They reported the measured density to be 3.55 g.cm.<sup>-3</sup> and calculated 3.56 g.cm.<sup>-3</sup> with 3 formula units in the rhombohedral unit cell. Staritzky (1956) also reported the space group of KAg(CN)<sub>2</sub> to be P31c rather than P31c as reported by Hoard (1933). The assignment of non-centrosymmetric space groups to these compounds was based entirely on the habit of the crystals, no piezoelectric effect having been observed. Newnham (1954) also failed to observe a piezoelectric effect in these compounds.

Because of the disagreement between Staritzky and Hoard as to the space group of  $KAg(CN)_2$ , Hoard's structure was critically re-examined. Several of the key intensities that Hoard used to establish his structure were measured with a Geiger counter. No inconsistencies were found, and it was concluded that Hoard's structure is correct insofar as the evidence from diffraction intensities is concerned.

There is, however, a slight modification of Hoard's structure which would give the non-centrosymmetric space group P31c. If the linear complex ion is slightly rotated out of the plane of the a and c axes, the center of symmetry no longer exists. Jones (1958) has examined thin plates of KAg(CN)<sub>2</sub> with polarized infrared radiation, and has concluded that if such a rota-

tion exists it cannot be more than about  $2^{\circ}$ . Because this rotation would involve only a small shift in positions of the carbon and nitrogen atoms, the effect on the X-ray intensities would be too small to observe experimentally. However, such a rotation could have a profound effect on the habit displayed by the crystals.

#### Experimental

A large number of crystals of KAu(CN)<sub>2</sub> were grown from water solution and from water solutions containing various amounts of acetone or ethyl alcohol. No marked change in habit was observed with changes in the proportions of these solvents. The usual habit was that of a steep rhombohedron  $\{10.1\}$ , sometimes modified by the pinacoid  $\{00.1\}$ , and the rhombohedron  $\{01\cdot 2\}$ . It was not uncommon, however, to find crystals with an apparent trigonal dipyramidal habit. Goniometric measurements showed that these forms have the same polar angle as the rhombohedron  $\{10.1\}$ . Crystals that were grown rapidly from saturated solutions formed long spike-like structures having numerous re-entrant angles and what appeared to be polysynthetic twin lamellae perpendicular to the caxis. Attempts to determine the true symmetry by the addition of dyes to the solution or by means of etch patterns were unsuccessful.

Precession photographs taken with Mo  $K\alpha$  radiation of the  $h0 \cdot l$  zone of crystals with rhombohedral habit were indexed on a hexagonal cell with the systematic restriction -h+k+l=3n indicating that the lattice is rhombohedral. Crystals with trigonal dipyramidal habit gave  $h0 \cdot l$  photographs which showed extra reflections that could not be indexed within the above restriction, but could be indexed within the restriction h-k+l=3n. Opposite ends of crystals of this habit yielded different photographs, one of which could be indexed according to -h+k+l=3n and the other according to h-k+l=3n. Obviously these crystals are twins, and *all* such crystals investigated were found to be twins. Twinning of this type cannot

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be detected by optical methods. Because Staritzky & Ellinger (1956) did not use single crystal X-ray techniques in their work, they were unaware that the non-centric crystals they observed were invariably twinned. Therefore, their selection of R3 as the space group of KAu(CN)<sub>2</sub> is not necessarily correct.

Attempts to grind spheres from single crystals of KAu(CN)<sub>2</sub> were not successful, spheroids elongated in the direction of the c axis being the usual result. Such a prolate spheroid,  $94\mu$  in diameter and  $134\mu$  long was used to obtain the intensity data. It was mounted on the c axis, and intensities were measured with a scintillation counter attached to a Weissenberg camera. Levels for l=0 through 17 were recorded, using Cu K $\alpha$ radiation. The three equivalent reflections (six on the zero level) were measured and their average value was taken as the observed intensity. Of the 364 nonequivalent reflections accessible with the instrument, 350 were observed to be greater than zero. Absorption corrections for a sphere of diameter  $114\mu$  were applied (Evans & Ekstein, 1952).

## **Determination of the structure**

Conversion of Staritzky & Ellinger's (1956) lattice constants for  $KAu(CN)_2$  to a hexagonal cell gives a=7.28 and c=26.36 Å. For the silver compound a = 7.40 and c = 17.59 Å (Staritzky, 1956). The a axes are nearly the same and the ratio of the c axes is ca.The similarity of the two hexagonal cells suggests that the structures are the same except for stacking of the layers. This guess is supported by the work of Jones (1954) who, by using polarized infrared radiation, found that the complex  $Au(CN)_2^-$  ion makes an angle of about  $28 \pm 1.8^{\circ}$  with the c axis, a value close to that found by Hoard for the  $Ag(CN)_2^-$  ion (27°).

Of the rhombohedral space groups having no systematic extinctions, only  $\overline{R3}$  or  $\overline{R3}$  can have configurations of linear complex ions that correspond to the layer configuration of  $KAg(CN)_2$ . As a trial structure, 9 formula units were placed in space group  $R\overline{3}$  as follows (hexagonal cell):

$$(0, 0, 0; \frac{1}{3}, \frac{2}{3}, \frac{2}{3}; \frac{2}{3}, \frac{1}{3}, \frac{1}{3}) + 3 K_1 \text{ in } a: (0, 0, 0) 6 K_2 \text{ in } b: \pm (0, 0, z)z \approx \frac{1}{3} 9 Au \text{ in } d: (\frac{1}{2}, 0, \frac{1}{2}; 0, \frac{1}{2}, \frac{1}{2}; \frac{1}{2}, \frac{1}{2}, \frac{1}{2}) 18 C \text{ in } f: \pm (x, y, z; \overline{y}, x - y, z; y - x, \overline{x}, z) with  $x = y = 0.355, z = 0.425$$$

and 18 N in f:

with x = y = 0.281, z = 0.386.

Because the only basis for assigning the space group R3 was the pseudo-morphology of the twinned crystals, and because the slight rotation of the linear complex ion which was postulated in order to destroy the center of symmetry of the silver compound does not destroy the center of symmetry of the structure in  $R\overline{3}$ , we believe that  $R\overline{3}$  is the correct space group.

The parameters of the trial structure were deduced by assigning a Au-C distance of 2.24 Å and a C-N distance of 1.15 Å to an assumed linear complex ion tilted  $28^{\circ}$  from the c axis. Qualitative examination of the structure factors showed that this trial structure was essentially correct. For example, the heavy atom contribution for the  $hh \cdot l$  reflections with h odd and l even is  $9f_{\rm K}$ - $3f_{\rm Au}$  resulting in a weak reflection, and for h and l even the contribution is  $9f_{K} + 9f_{Au}$  giving a strong reflection.

The trial parameters were used as initial values in a least-squares refinement on an IBM 704 computer. The form factors used for potassium, gold, and carbon and nitrogen were those of Berghuis et al. (1955), Henry (1954) and McWeeney (1951), respectively. Isotropic temperature factors were assigned to each crystallographically different atom. A separate scale factor was used for each value of l because intensities had been measured for only the c axis mounting, and interlayer scaling was therefore impossible. All reflections were weighted equally. The final R factor was 10.5%. The observed and calculated structure factors are given in Table 1 and the final parameters are in Table 2. The maximum deviation of the 18 scale factors from their mean was 10.5% and their mean deviation was 3.4%.

A three-dimensional Fourier was computed in the regions of the various atoms. The carbon and nitrogen atoms were not resolved from the diffraction ripples surrounding the gold atom. However, a three-dimensional Fourier with the gold contribution subtracted from the observed structure factors did show resolved

## Table 1. Observed and calculated structure factors for KAu(CN)<sub>2</sub>.

The column headings are  $h, k, l, F_o$  and  $F_c$ 

 Table 2. Parameters from the least-squares refinement of

 KAu(CN)<sub>2</sub>

		•	•	$B  imes 10^{16}$
$\mathbf{A}_{\mathbf{tom}}$	1 <i>x</i>	$\boldsymbol{y}$	z	$\mathrm{em.}^2$
К,	0	0	0	$2{\cdot}11\pm0{\cdot}37$
$\mathbf{K}_{2}$	0	0	$0.3441 \pm 0.0007$	$1{\cdot}87\pm0{\cdot}24$
$\mathbf{A}\mathbf{\tilde{u}}$	$\frac{1}{2}$	0	1/2	$2{\cdot}96 \pm 0{\cdot}04$
$\mathbf{C}$	$0.403 \pm 0.009$	$0.406 \pm 0.009$	$0.424 \pm 0.003$	$5 \cdot 56 \pm 1 \cdot 40$
$\mathbf{N}$	$0{\cdot}337\pm0{\cdot}009$	$0.348 \pm 0.009$	$0.383 \pm 0.003$	$7 \cdot 62 \pm 1 \cdot 60$

carbon and nitrogen peaks at  $x_c = 0.410$ ,  $y_c = 0.418$ ,  $z_0 = 0.430$ ,  $x_N = 0.336$ ,  $y_N = 0.363$  and  $z_N = 0.393$  in reasonable agreement with the least-squares results. A composite of three-dimensional sections through the atoms is shown in Fig. 1. The asymmetry of these



Fig. 1. Composite of electron-density sections through the atoms of  $KAu(CN)_2$ . The gold atom contours are from the  $F_o$  Fourier. The other contours are from the Fourier with the gold atom removed. The initial contour about  $K_1$ ,  $K_2$ , and Au is at g=0 electrons/Å<sup>3</sup> and is at g=0.5 about C and N. The contour interval for C and N is 0.5 electrons, 5 electrons for K, and  $K_2$  and 20 electrons for Au.

peaks is caused by the limited nature of the data, i.e.  $l \leq 17$  and no reflections of the type 00l.

#### Accuracy of the structure

The standard deviations given in Table 2 have been computed from the usual formula

$$\sigma(\xi_i) = \left[\frac{\Sigma(\varDelta F)^2}{(m-s)\Sigma\left(\frac{\partial F}{\partial \xi_i}\right)^2}\right]^{\frac{1}{2}}$$

where m is the number of observations and s is the number of parameters. Unfortunately, because of the large temperature factors of carbon and nitrogen their positions are subject to a larger error than anticipated. The interatomic distances (Table 3) are all quite reasonable, and the C-N distance of 1.17 Å, although subject to a large standard deviation, nevertheless is found to be very close to that observed in other cyanide compounds.

## Discussion of the structure

The structure of  $KAu(CN)_2$  is essentially the same as that of  $KAg(CN)_2$  and is made up of layers of potassium ions alternating with layers of complex ions, each pair of layers being shifted  $\frac{1}{3}$  the length of the long diagonal of the cell base. This shift of the layers gives rise to a rhombohedral primitive cell. In the silver compound the shift is  $\frac{1}{2}$  the length of the diagonal, and thus the cell is hexagonal. A drawing of a portion of the unit cell is given in Fig. 2. Bonding between layers is such



Fig. 2. A drawing of a portion of the unit cell of KAu(CN)<sub>2</sub>.

as to result in little if any cleavage parallel to the layers. However, bonding within layers is weak, and complex ions can be 'peeled' from the sides with relative ease. This gives a qualitative explanation for the failure to grind spheres. It is of interest to note that attempts to grind spheres of  $KAg(CN)_2$  also yielded prolate spheroids.

Table 3. Interatomic distances and angles in KAu(CN)<sub>2</sub>

$K_{1}-N$ (6)	$2 \cdot 79 \pm 0 \cdot 14$ Å	∠ Au–C–N	$172{\cdot}8\pm7{\cdot}5^{\circ}$
$K_{2} - N(3)$	$2 \cdot 70 \pm 0 \cdot 14$	$\angle c$ axis–Au–N	$20.4 \pm 2.9$
$\bar{K_{2}}-N'(3)$	$2 \cdot 83 \pm 0 \cdot 14$	$\angle c  ext{ axis-Au-C}$	$19.5 \pm 4.4$
Au–C	$2 \cdot 12 \pm 0 \cdot 14$		
C–N	$1.17 \pm 0.20$		

The interatomic distances and angles are given in Table 3. The angle between the complex ion and the c axis is smaller than that found by Hoard in KAg(CN)<sub>2</sub> and is also smaller than the one Jones (1954) found in his infrared study of KAu(CN)<sub>2</sub>. Our results are subject to fairly large error. Jones (1954, 1958) did not consider certain possible systematic errors so that his estimate of an error of  $1.8^{\circ}$  is perhaps small.

Our results, therefore, differ from Jones' by only a possibly significant amount. The smaller tilt that we find has the virtue of making the K-N distances more nearly equal than those found by Hoard. Hoard observed a particularly short K-N distance of 2.58 Å. Our results do not answer the question of whether the complex ion is rotated out of the plane of the *a* and *c* axes. Because of its significance in assigning the proper space group to KAg(CN)<sub>2</sub>, an answer to this question was really the main object of our work. The criteria for the ion to lie in the plane is that  $x_{\rm C}=y_{\rm C}$  and  $x_{\rm N}=y_{\rm N}$ . The parameters for nitrogen differ by a little more than one standard deviation, but this is not a significant difference.

The habit of the twinned crystals indicates that the composition plane, which is perpendicular to the c axis, is a mirror for the twinned individuals insofar as the forms observed are concerned. The two operations which would produce this condition are rotations of 180° about the zone axes  $[00\cdot1]$  and  $[1\overline{1}\cdot0]$ . In the point group  $\overline{3}$ , rotation about  $[00\cdot1]$  would result in a mirror with regard to all forms  $(hk\cdot l)$ , while rotation about  $[1\overline{1}\cdot0]$  would result in a mirror for forms of the type  $(h0\cdot l)$ ,  $(0k\cdot l)$ , and  $\{hh\cdot l\}$  but not generally for  $\{hk\cdot l\}$ . Because the only forms observed are  $\{10\cdot1\}$  and  $\{01\cdot2\}$ , the morphology yields no information as to the choice of twin operations.

In examining the structure with regard to the two rotational operations above, it is further necessary to consider the location of the composition plane. It may be placed at the height z=0 so that the potassium ions are in or near the composition plane, or it may be placed at the height  $z=\frac{1}{2}$  so that the gold atoms lie in the composition plane, Rotation about [00·1] with the composition plane at z=0 changes the near octahedral configuration of nitrogen about potassium to one where the nitrogens lie at the corners of a distorted trigonal prism with the potassium at its center. Placing the composition plane at  $z=\frac{1}{2}$  results in a non-linear complex at the twin boundary. Rotation about  $[1\overline{1} \cdot 0]$  with the composition plane at z=0results in a slight distortion of the configuration of nitrogens about potassium but it remains essentially octahedral. The gold atoms now lie at a distance c/3across the twin boundary and, since some of the potassiums are slightly displaced from z=0, not all the atoms at or near the composition plane are properly oriented for either member of the twin. Placing the twin plane at  $z=\frac{1}{2}$  does not alter the nitrogenpotassium configuration at all, and does not affect the complex if it is assumed to lie in the *a*-*c* plane.

The configuration of a single crystal may be regarded as representing a minimum free energy state for the particles involved (Buerger, 1945). This condition is influenced primarily by the first sphere of coordination or nearest neighbors of an atom, subsequent spheres of coordination having less and less influence. For twinning to occur, it must be possible to change the orientation of part of the structure with but a slight deviation from the minimum free energy condition. The last twinning operations discussed, rotation about  $[1\overline{1}\cdot 0]$  with the composition plane at  $z=\frac{1}{2}$ , satisfies this requirement. There is no change in the nitrogenpotassium configuration, no distortion of the complex ion, and the complex ions and potassium ions at and adjacent to the composition plane are in proper position for either orientation.

No such twinning can occur in the analogous silver compound in which, being hexagonal, the only permissible operations result in identity. Furthermore, it is noted that the non-centrosymmetric habit of some crystals of KAg(CN)<sub>2</sub> observed by Staritzky cannot be explained as a result of twinning, and, hence, the space group P31c is probably correct. A small but real rotation of the silver dicyanide complex from the a-c plane is probably present, and this condition in the structure would further hamper the possibility of twinning.

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